## ${ }^{\text {ST }} 10$

- Grab a graphing calculator
- Grab a new note packet
- Find all your homework for Unit 9 and put it in order of Days (Days 1-9)
- Find your grade sheet on the side table and highlight every grade you are not happy with.
- What can you start doing in this unit that will make you proud of yourself?


# DAY 1: GRAPHING EXPONENTIAL FUNCTIONS 

Unit 10: Exponential Functions

## EXPLORING

Exploring with Graphs: Graph the following equations:
A. $\mathrm{y}=\mathrm{x}$

| $\mathbf{x}$ | -3 | -2 | -1 | 0 | 1 | 2 | 3 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{y}$ |  |  |  |  |  |  |  |

b. $y=x^{2}$

| $\mathbf{x}$ | -3 | -2 | -1 | 0 | 1 | 2 | 3 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{y}$ |  |  |  |  |  |  |  |

C. $y=2 x$

| $\mathbf{x}$ | -3 | -2 | -1 | 0 | 1 | 2 | 3 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{y}$ |  |  |  |  |  |  |  |



Type: $\qquad$


Type:


Type: $\qquad$

How is Equation C different from Equations $A$ and $B$ (you have already learned about equations $A$ \& $B$ ).

## EXPLORING

## Exploring with a Scenario:

Which of the options below will make you the most money after 15 days?
a. Earning $\$ 100$ a day?

| $\mathbf{x}$ | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{y}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

b. Earning a penny at the end of the first day, earning two pennies at the end of the second day, earning 4 pennies at the end of the third day, earning 8 pennies at the end of the fourth day, and so on?

| $\mathbf{x}$ | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{y}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

## EXPONENTIAL FUNCTIONS

## Exponential functions <br> $$
y=a b^{x}
$$

1. Variable is in the power (exponent) versus the base
2. Start small and increase quickly or vice versa
3. Asymptotes (heads towards a horizontal line but never touches it)
4. Constant Ratios (multiply by same number every time)


## ASYMPTOTES

An asymptote is a line that an exponential graph gets closer and closer to but never touches or crosses. The equation for the line of an asymptote for a function in the form of $f(x)=a b x$ is always $y=$ $\qquad$ .

Identify the asymptote of each graph.
a.
b.


c.


## ASYMPTOTES

d.

e.

f.


## EVALUATING FUNCTIONS

- When graphing exponential functions, it is important that you understand how to evaluate an exponential function.
- Since the variable is in the exponent, you will evaluate the function differently that you did with a linear function. You will still substitute the value of $x$ into the function, but will be taking that value as a power.
Example 1: Evaluate each exponential function.
a. $f(x)=2(3)^{x}$ when $x=5$
b. $\mathrm{y}=8(0.75)^{\mathrm{x}}$ when $\mathrm{x}=3$
c. $f(x)=4^{x}$, find $f(2)$.


## GENERAL FORM

The general form of an exponential function is:

## $y=a b^{x}$

Where a represents your starting or initial value/population and y-intercept

## GRAPHING EXPONENTIAL FUNCTIONS

## Graphing Exponential Functions Steps

1. Create an $x-y$ chart with 5 values for $x$ (Safest values for $\mathrm{x}:-2,-1,0,1,2$ ).
2. Substitute those values into the function and record the $y$ or $f(x)$ values.
3. Graph each ordered pair on a graph.

Graph the following:
a. $y=3(4)^{x}$

## EXAMPLE 1



EXAMPLE 1
Graph the following:
a. $y=3(1)$

| $x$ | $y$ |
| :--- | :--- |
| -3 | .05 |
| -2 | $: 1875$ |
| -1 | $: 752^{24}$ |
| 0 | $32^{x 4}$ |
| 1 | $1122^{24}$ |
|  | $48^{2 \times 4}$ |



## EXAMPLE 2

Graph the following:
b. $f(x)=2^{x}$


Y-intercept:
Asymptote:

$$
y=a b^{x}
$$

EXAMPLE 2
Graph the following:

$$
\begin{aligned}
& \text { b. } f(x)=x^{2 x}=1_{a}^{1}(2)^{x}
\end{aligned}
$$




Graph the following:
c. $y=3\left(\frac{1}{2}\right)^{x}$

## EXAMPLE 3



EXÂMPLE 3
Graph the following:



## EXAMPLE 4

Graph the following:
d. $f(x)=4(.25)^{x}$


## THE Y-INTERCEPT

Think about it...
What did you notice about the y-intercept and the equation?

You have two ways you can find the $y$-intercept when given an equation: $y=3(4)^{x}$
a. $\qquad$
b. $\qquad$

## SUMMARY

| Equation | 'a' values | 'b' values | General Shape of Graph |
| :---: | :---: | :---: | :---: |
| $y=3(4)^{x}$ |  |  |  |
| $f(x)=2^{x}$ |  |  |  |
| $y=3\left(\frac{1}{2}\right)^{x}$ |  |  |  |
| $f(x)=4(.25)^{x}$ |  |  |  |

## IDENTIFYING GROWTH/DECAY

$$
\text { a. } y=4(3 / 4)^{x}
$$

b. $y=-2(3)^{x}$
c. $y=1 / 2(1.4)^{x}$
d. $y=(0.9)^{x}$
e. $y=3\left(\frac{5}{2}\right)^{x}$

