

Name _____

Date _____

Day 1 – SOLVING EQUATIONS WITH VARIABLES ON BOTH SIDES

Goal: Get ONE variable alone on one side of = sign.

1. Use Distributive Property, if necessary.
2. Combine like terms, if necessary
3. Move one variable by adding its inverse to both sides of =.
4. Solve as usual.

1.

$$12k + 15 = 35 + 2k$$

Original problem

$$\begin{array}{r} -2k \qquad \qquad -2k \\ \hline 10k + 15 = 35 \end{array}$$

Move variables to one side.

$$10k + 15 = 35$$

$$\begin{array}{r} -15 \quad -15 \\ \hline 10k = 20 \end{array}$$

Eliminate adding or subtracting

$$\frac{10k}{10} = \frac{20}{10}$$

Eliminate multiplying or dividing

$$k = 2$$

$$k = 2$$

Solution! Remember...Check Your Answer!

2.

$$3(a + 22) = 12a + 30$$

Original Problem

$$3a + 66 = 12a + 30$$

Do the Distributive Property First!!!

$$\begin{array}{r} -3a \qquad \qquad -3a \\ \hline 66 = 9a + 30 \end{array}$$

Move Variables to one Side.

$$66 = 9a + 30$$

$$\begin{array}{r} -30 \qquad \qquad -30 \\ \hline 36 = 9a \end{array}$$

Eliminate adding or subtracting

$$\frac{36}{9} = \frac{9a}{9}$$

Eliminate multiplying or dividing

$$4 = a$$

Solution! Remember...Check Your Answer!

3.

$$3(x + 1) - 5 = 5x - 2$$

Original Problem

$$3x + 3 - 5 = 5x - 2$$

Do the Distributive Property First!!!

$$3x - 2 = 5x - 2$$

Combine Like Terms

$$\begin{array}{r} -3x \qquad \qquad -3x \\ \hline -2 = 2x - 2 \end{array}$$

Move Variables to one Side.

$$-2 = 2x - 2$$

$$\begin{array}{r} +2 \qquad \qquad +2 \\ \hline 0 = 2x \end{array}$$

Eliminate adding or subtracting

$$\frac{0}{2} = \frac{2x}{2}$$

Eliminate multiplying or dividing

$$0 = x$$

Solution! Remember...Check Your Answer!

Try These!!!

4. $5x = -7x + 6$

5. $7 - 3x = x - 4(2 + x)$

HMMM.....Take a look at the following examples:

6. $6(4x - 5) = 24x - 30$

7. $5(3x + 5) = 3(5x + 1)$

The Rules:

- When you solve an equation and you end with a **true statement**, the solution set will be: _____.

Example:

$$\begin{array}{r} 3(x + 2) = 3x + 6 \\ 3x + 6 = 3x + 6 \\ -3x \quad -3x \\ \hline 6 = 6 \end{array}$$

Many Solutions!

- When you solve an equation and you end with a **false statement**, the solution set will be: _____.

$$\begin{array}{r} 3(x + 2) = 3x + 4 \\ 3x + 6 = 3x + 4 \\ -3x \quad -3x \\ \hline 6 \neq 4 \end{array}$$

No Solutions!

Try These:

8. $2x + 5 = 2x - 3$

9. $3(x+1) - 5 = 3x - 2$

Class Practice:

10. $6x + 7 = 8x - 13$

11. $6(y + 2) - 4 = -10$

12. $4(2x - 8) = 3(2 - 3x)$

13. $4(r + 20) = 1/5(20r + 400)$

14. $-2x = -3x + 12 - 2x$

15. $8(b + 1) + 4 = 3(2b - 8) - 16$

