

★ UNIT 3: MODELING AND ANALYZING QUADRATIC FUNCTIONS ★

A) Unit 3: Interpret the Structure of Expressions

$$a^2 - b^2 = (a+b)(a-b)$$

1. Which expression is equivalent to $121x^2 - 64y^2$?

- A. $(11x - 16y)(11x + 16y)$
- B. $(11x - 16y)(11x - 16y)$
- C. $(11x + 8y)(11x + 8y)$
- D. $(11x + 8y)(11x - 8y)$

$$a = 11x$$

$$b = 8y$$

2. What is a common factor for the expression $24x^2 + 16x + 144$?

- A. 16
- B. $8x$
- C. $3x^2 + 2x + 18$
- D. $8(x - 2)(3x^2 + 9)$

$$\underline{8}$$

3. Which of these shows the complete factorization of $6x^2y^2 - 9xy - 42$?

- A. $3(2xy^2 - 7)(xy^2 + 2)$
- B. $(3xy + 6)(2xy - 7)$
- C. $3(2xy - 7)(xy + 2)$
- D. $(3xy^2 + 6)(2xy^2 - 7)$

$$3(2x^2y^2 - 3xy - 14)$$

$$a = 2 \quad b = -3 \quad c = 14$$

$$ac = 28$$

~~$$\begin{array}{r} -28 \\ 4 \quad -7 \\ -3 \end{array}$$~~

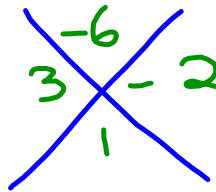
	$2xy$	-7
xy	$2x^2y^2$	$-7xy$
2	$4xy$	-14

$$= 3(2xy - 7)(xy + 2)$$

B) Unit 3: Write Expressions in Equivalent Forms to Solve Problems

1. What are the zeros of the function represented by the quadratic expression $2x^2 + x - 3$? $a=2$ $b=1$ $c=-3$

- A. $x = -\frac{3}{2}$ and $x = 1$
- B. $x = -\frac{2}{3}$ and $x = 1$
- C. $x = -1$ and $x = \frac{2}{3}$
- D. $x = -1$ and $x = -\frac{3}{2}$



$a=2$ $b=1$ $c=-3$
 $ac = -6$

$2x^2$	$-2x$	$x-1=0$ $x=1$
$3x$	-3	$2x+3=0$ $x=-\frac{3}{2}$

$(x-1)(2x+3) = 0$

2. What is the vertex of the graph of $f(x) = x^2 + 10x - 9$? $a=1$ $b=10$

- A. (5, 66)
- B. (5, -9)
- C. (-5, -9)
- D. (-5, -34)

$x = \frac{-b}{2a} = \frac{-10}{2(1)} = -5$
 $f(-5) = (-5)^2 + 10(-5) - 9$
 $25 - 50 - 9$

3. Which of these is the result of completing the square for the expression

- $x^2 + 8x - 30$
- A. $(x + 4)^2 - 30$
 - B. $(x + 4)^2 - 46$
 - C. $(x + 8)^2 - 30$
 - D. $(x + 8)^2 - 94$

$x^2 + 8x - 30 = 0$
 $+30 \quad +30$

$x^2 + 8x = 30$
 $\frac{8}{2} = (4)^2 = 16$

$x^2 + 8x + 16 = 30 + 16$
 $(x + 4)^2 = 46$
 $(x + 4)^2 - 46$

4. The expression $-x^2 + 70x - 600$ represents a company's profit for selling x items. For which number(s) of items sold is the company's profit equal to \$0?

A. 0 items

B. 35 items

C. 10 items and 60 items

D. 20 items and 30 items

$$-x^2 + 70x - 600 = 0$$

C) Unit 3: Create Equations That Describe Numbers or Relationships

1. A garden measuring 8 feet by 12 feet will have a walkway around it. The walkway has a uniform width, and the area covered by the garden and the walkway is 192 square feet. What is the width of the walkway?

A. 2 feet

B. 3.5 feet

C. 4 feet

D. 6 feet

2. The formula for the area of a circle is $A = \pi r^2$. Which equation shows the formula in terms of r ?

A. $r = \frac{2A}{\pi}$

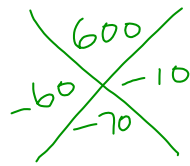
B. $r = \frac{\sqrt{A}}{\pi}$

C. $r = \sqrt{\frac{A}{\pi}}$

D. $r = \frac{A}{2\pi}$

$$\textcircled{4} \quad (-x^2 + 70x - 600 = 0) - 1$$

$$x^2 - 70x + 600 = 0$$



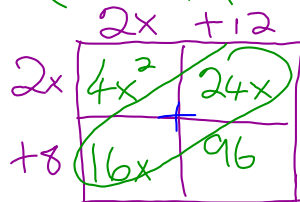
$$(x - 60)(x - 10) = 0$$

①



$$L = 12 + 2x \quad w = 8 + 2x$$

$$(2x + 12)(2x + 8)$$

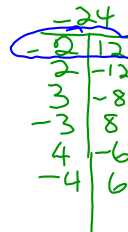
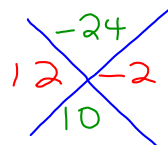


$$4x^2 + 40x + 96 = 192$$

$$\underline{-192 \quad -192}$$

$$4x^2 + 40x - 96 = 0$$

$$4(x^2 + 10x - 24) = 0$$



$$4(x + 12)(x - 2) = 0$$

↓

$$x + 12 = 0 \quad \text{or} \quad x - 2 = 0$$

$$\underline{-12 \quad -12} \quad \text{or} \quad \underline{+2 \quad +2}$$

$$x = -12 \quad \text{or} \quad x = 2$$

$$\textcircled{2} \quad A = \pi r^2$$

$$\frac{A}{\pi} = \frac{\pi r^2}{\pi}$$

$$\sqrt{\frac{A}{\pi}} = \sqrt{r^2}$$

$$\sqrt{\frac{A}{\pi}} = r$$

D) Unit 3: Solve Equations and Inequalities in One Variable

1. What are the solutions to the equation $2x^2 - 2x - 12 = 0$?

- A. $x = -4, x = 3$
 B. $x = -3, x = 4$
 C. $x = -2, x = 3$
 D. $x = -6, x = 2$

$$2(x^2 - x - 6) = 0$$

~~$$\begin{array}{r} -6 \\ 2 \times -3 \\ -1 \end{array}$$~~

$$2(x+2)(x-3) = 0$$

$$\begin{array}{cc} \downarrow & \downarrow \\ x = -2 & x = 3 \end{array}$$

2. What are the solutions to the equation $6x^2 - x - 40 = 0$?

- A. $x = -\frac{8}{3}, x = -\frac{5}{2}$
 B. $x = -\frac{8}{3}, x = \frac{5}{2}$
 C. $x = \frac{5}{2}, x = \frac{8}{3}$
 D. $x = -\frac{5}{2}, x = \frac{8}{3}$

$$a = 6 \quad b = -1 \quad c = -40$$

$$x = \frac{-(-1) \pm \sqrt{(-1)^2 - 4(6)(-40)}}{2(6)}$$

$$x = \frac{1 \pm 31}{12} = x = \frac{1+31}{12} \text{ or } \frac{1-31}{12}$$

$$= x = \frac{8}{3} \text{ or } -\frac{5}{2}$$

3. What are the solutions to the equation $x^2 - 5x = 14$?

- A. $x = -7, x = -2$
 B. $x = -14, x = -1$
 C. $x = -2, x = 7$
 D. $x = -1, x = 14$

$$x^2 - 5x - 14 = 0$$

~~$$\begin{array}{r} -14 \\ 2 \times -7 \\ -5 \end{array}$$~~

$$(x+2)(x-7) = 0$$

$$\begin{array}{cc} \downarrow & \downarrow \\ x = -2 & x = 7 \end{array}$$

4. An object is thrown in the air with an initial velocity of 5 m/s from a height of 9 m. The equation $h(t) = -4.9t^2 + 5t + 9$ models the height of the object in meters after t seconds.

About how many seconds does it take for the object to hit the ground? Round your answer to the nearest tenth of a second.

- A. 0.940 second
 B. 1.50 seconds
 C. 2.00 seconds
 D. 9.00 seconds

$a = -4.9$ $b = 5$ $c = 9$
 Use Quadratic Formula

$$t = \frac{-5 \pm \sqrt{5^2 - 4(-4.9)(9)}}{2(-4.9)}$$

$$t = \frac{-5 \pm 14.2}{-9.8} = -0.94 \text{ or } 1.96 \approx 2 \text{ seconds}$$

E) Unit 3: Build a Function That Models a Relationship between Two Quantities

1. Which statement BEST describes the graph of $f(x + 6)$?
- A. The graph of $f(x)$ is shifted up 6 units.
 B. The graph of $f(x)$ is shifted left 6 units.
 C. The graph of $f(x)$ is shifted right 6 units.
 D. The graph of $f(x)$ is shifted down 6 units.
2. Which of these is an even function?
- A. $f(x) = 5x^2 - x$
 B. $f(x) = 3x^3 + x$
 C. $f(x) = 6x^2 - 8$
 D. $f(x) = 4x^3 + 2x^2$
3. Which statement BEST describes how the graph of $g(x) = -3x^2$ compares to the graph of $f(x) = x^2$?
- A. The graph of $g(x)$ is a vertical stretch of $f(x)$ by a factor of 3.
 B. The graph of $g(x)$ is a reflection of $f(x)$ across the x -axis.
 C. The graph of $g(x)$ is a vertical shrink of $f(x)$ by a factor of $\frac{1}{3}$ and a reflection across the x -axis.
 D. The graph of $g(x)$ is a vertical stretch of $f(x)$ by a factor of 3 and a reflection across the x -axis.

F) Unit 3: Interpret Functions That Arise in Applications in Terms of the Context

1. A flying disk is thrown into the air from a height of 25 feet at time $t = 0$. The function that models this situation is $h(t) = -16t^2 + 75t + 25$, where t is measured in seconds and h is the height in feet. What values of t best describe the times when the disk is flying in the air?

- A. $0 < t < 5$
 B. $0 < t < 25$
 C. all real numbers
 D. all positive integers

$$a = -16 \quad b = 75 \quad c = 25$$

$$t = \frac{-75 \pm \sqrt{75^2 - 4(-16)(25)}}{2(-16)} = \frac{-75 \pm 85}{-32}$$

$$= -0.3125 \text{ or } 5$$

2. Use this table to answer the question.

	x	f(x)
x_1	-2	15
	-1	9
x_2	0	5
	1	3
	2	3

$$AROC = \frac{y_2 - y_1}{x_2 - x_1}$$

$$= \frac{5 - 15}{0 - (-2)}$$

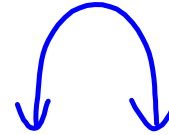
$$= \frac{-10}{2} = -5$$

What is the average rate of change of x over the interval $-2 \leq x \leq 0$?

- A. -10
 B. -5
 C. 5
 D. 10

3. What is the end behavior of the graph of $f(x) = -0.25x^2 - 2x + 1$?

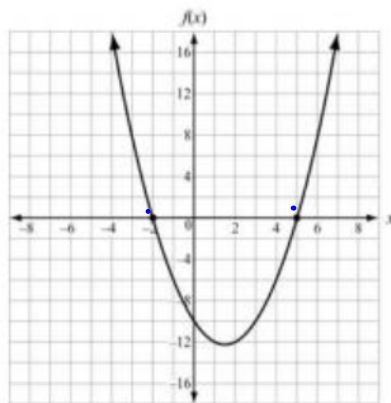
- A. As x increases, $f(x)$ increases.
As x decreases, $f(x)$ decreases.
- B.** As x increases, $f(x)$ decreases.
As x decreases, $f(x)$ decreases.
- C. As x increases, $f(x)$ increases.
As x decreases, $f(x)$ increases.
- D. As x increases, $f(x)$ decreases.
As x decreases, $f(x)$ increases.



G) Unit 3: Analyze Functions Using Different Representations

1. Use this graph to answer the question.

Roots are
 $x = -2, 5$



Which function is shown in the graph?

- A.** $f(x) = x^2 - 3x - 10$
- B. $f(x) = x^2 + 3x - 10$
- C. $f(x) = x^2 + x - 12$
- D. $f(x) = x^2 - 5x - 8$

~~$$\begin{array}{r} -10 \\ 2 \quad -5 \\ -3 \end{array}$$~~

$$(x+2)(x-5) = 0$$

\downarrow \downarrow
 $x = -2$ $x = 5$

2. The function $f(t) = -16t^2 + 64t + 5$ models the height of a ball that was hit into the air, where t is measured in seconds and h is the height in feet.

This table represents the height, $g(t)$, of a second ball that was thrown into the air.

Time, t (in seconds)	Height, $g(t)$ (in feet)
0	4
1	36
2	36
3	4

Which statement BEST compares the length of time each ball is in the air?

- A. The ball represented by $f(t)$ is in the air for about 5 seconds, and the ball represented by $g(t)$ is in the air for about 3 seconds.
- B. The ball represented by $f(t)$ is in the air for about 3 seconds, and the ball represented by $g(t)$ is in the air for about 5 seconds.
- C. The ball represented by $f(t)$ is in the air for about 3 seconds, and the ball represented by $g(t)$ is in the air for about 4 seconds.
- D. The ball represented by $f(t)$ is in the air for about 4 seconds, and the ball represented by $g(t)$ is in the air for about 3 seconds.

★ UNIT 4: MODELING AND ANALYZING EXPONENTIAL FUNCTIONS ★

A) Unit 4: Create Equations That Describe Numbers or Relationships

1. A certain population of bacteria has an average growth rate of 2%. The formula for the growth of the bacteria's population is $A = P_0 \cdot 1.02^t$, where P_0 is the original population and t is the time in hours. $.02 + 1$

If you begin with 200 bacteria, about how many bacteria will there be after 100 hours?

- A. 7
B. 272
C. 1,449
D. 20,000

$$A = 200(1.02)^{100}$$

B) Unit 4: Build a Function That Models a Relationship Between Two Quantities

1. Which function represents this sequence?

n	1	2	3	4	5	...
a_n	6	18	54	162	486	...

- A. $f(n) = 3^{n-1}$
B. $f(n) = 6^{n-1}$
C. $f(n) = 3(6^{n-1})$
D. $f(n) = 6(3^{n-1})$

$$a_n = a_1 \cdot (r)^{n-1}$$

$$a_n = a_1 \cdot r^{n-1}$$

$$a_1 = 6 \quad r = \frac{18}{6} = 3$$

$$a_n \text{ or } f(n) = 6 \cdot 3^{n-1}$$

2. The points (0, 1), (1, 5), (2, 25), and (3, 125) are on the graph of a function. Which equation represents that function?

- A. $f(x) = 2^x$
B. $f(x) = 3^x$
C. $f(x) = 4^x$
D. $f(x) = 5^x$

1, 5, 25, 125 $r = 5$
 $1 \cdot 5^x$

C) Unit 4: Build New Functions from Existing Functions

1. Which function shows the function $f(x) = 3^x$ being translated 5 units to the left?

- A. $f(x) = 3^x - 5$
B. $f(x) = 3^{(x+5)}$
C. $f(x) = 3^{(x-5)}$
D. $f(x) = 3^x + 5$

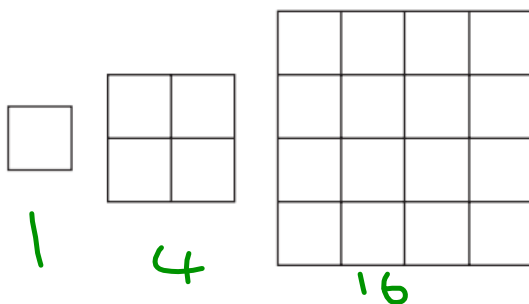
2. Which function shows the function $f(x) = 3^x$ being translated 5 units down?

- A. $f(x) = 3^x - 5$
B. $f(x) = 3^{(x+5)}$
C. $f(x) = 3^{(x-5)}$
D. $f(x) = 3^x + 5$

D) Unit 4: Understand the Concept of a Function and Use Function Notation

$$y = a \cdot b^x$$

1. Consider this pattern.



Which function represents the sequence that represents the pattern?

- A. $a_n = (4)^{(n-1)}$
- B. $a_n = (4)^{(a_n-1)}$
- C. $a_n = (a_n)(4)^{(n-1)}$
- D. $a_n = (a_n)^4$

$$r = 4$$

3. Which explicit formula describes the pattern in this table?

d	C
0	1
1	6
2	36
3	216

- A. $C = 6d$
- B. $C = d + 6$
- C. $C = 6^d$
- D. $C = d^6$

2. Which function is modeled in this table?

x	f(x)
1	1000
2	800
3	640
4	512

- A. $f(x) = 1,000(0.80)^x$
- B. $f(x) = 1,000(0.20)^x$
- C. $f(x) = 1,000(0.80)^{x-1}$
- D. $f(x) = 1,000(0.20)^{x-1}$

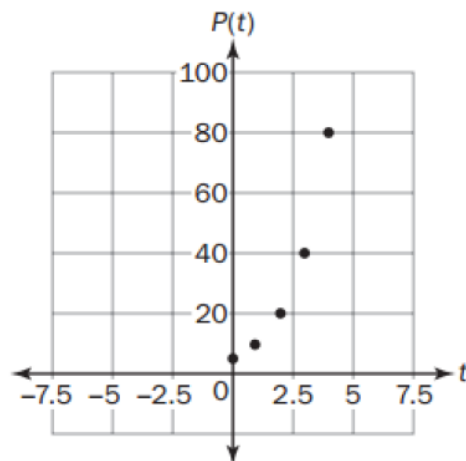
$$r = \frac{800}{1000} = .80$$

4. If $f(12) = 100(0.50)^{12}$, which expression gives $f(x)$?

- A. $f(x) = 0.50^x$
- B. $f(x) = 100^x$
- C. $f(x) = 100(x)^{12}$
- D. $f(x) = 100(0.50)^x$

E) Unit 4: Interpret Functions That Arise in Applications in Terms of the Context

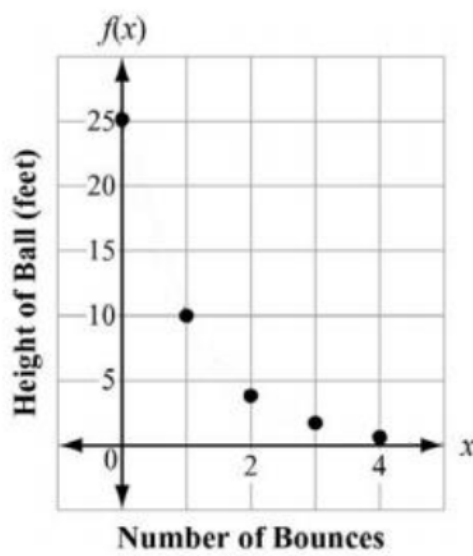
1. A population of squirrels doubles every year. Initially, there were 5 squirrels. A biologist studying the squirrels created a function to model their population growth: $P(t) = 5(2^t)$, where t is the time in years. The graph of the function is shown.



What is the range of the function?

- A. any real number
- B. any whole number greater than 0
- C. any whole number greater than 5
- D. any whole number greater than or equal to 5**

2. The function graphed on this coordinate grid shows $f(x)$, the height of a dropped ball in feet after its x th bounce.



On which bounce was the height of the ball 10 feet?

- A. bounce 1
- B. bounce 2
- C. bounce 3
- D. bounce 4