

Warm-Up 1/31/18

Factor the following:

1. $4x + 16$

$$\frac{\cancel{4}x + 16}{\cancel{4}} = \frac{\quad}{4}$$

2. $x^2 + 14x + 33$

$$4 \cdot (x + 4)$$

$$(x+3)(x+11)$$

~~33
3 11
14~~

3. $4x^2 + 12x + 9$ ac = 36 b = 12

~~36

6 6

12~~

$2x \quad 3$
 $2x \quad 3$

$4x^2$	$6x$
$6x$	9

$(2x+3)(2x+3) = (2x+3)^2$

4. $3x^2 - 10x + 8$

~~24

-6 -4

-10~~

$3x - 4$
 x

$3x^2$	$-4x$
$-6x$	8

$(3x-4)(x-2)$

factored out. It is usually easier to factor out GCF first.

$$\frac{3x^2}{3} - \frac{6x}{3} + \frac{3}{3}$$

~~$$\begin{array}{r} 1 \\ -1 \quad -1 \\ -2 \end{array}$$~~

$$3(x^2 - 2x + 1)$$

$$a=1 \quad b=-2 \quad c=1$$

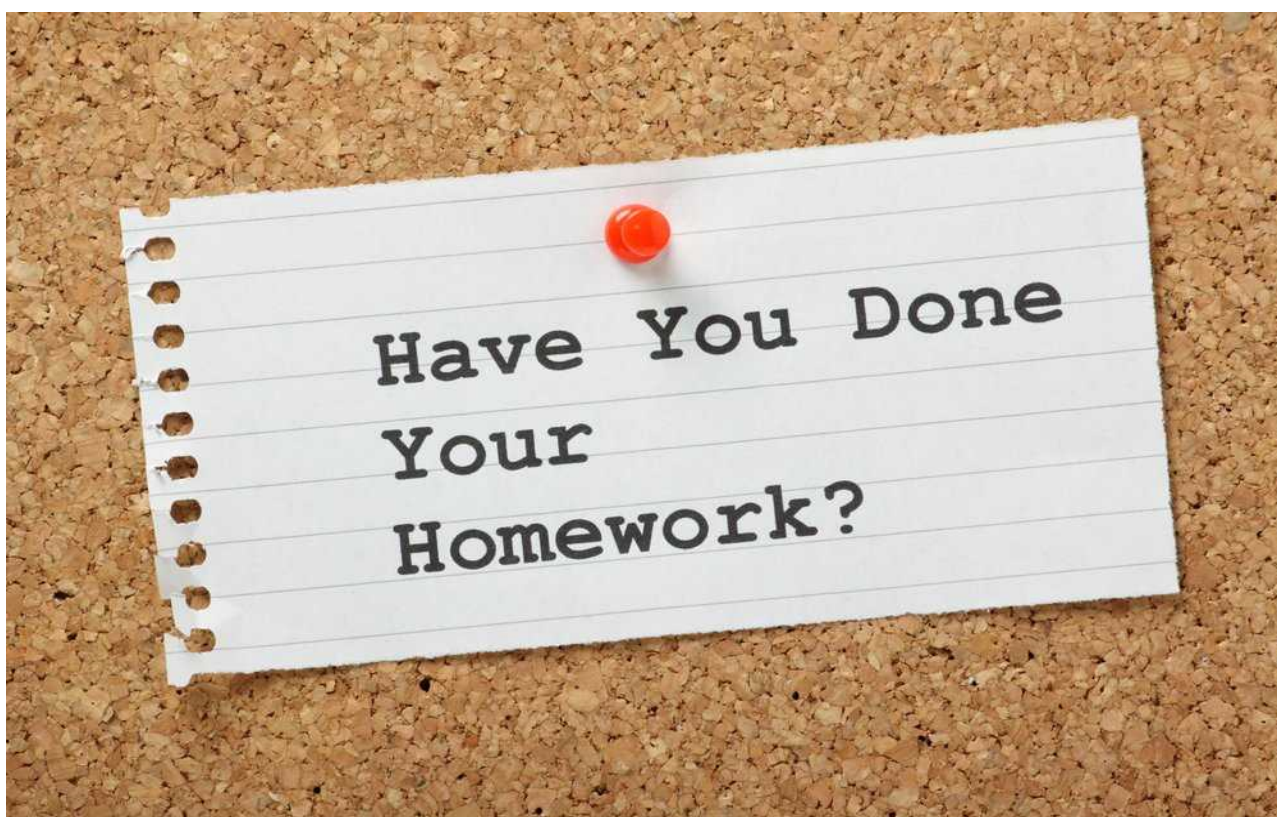
$$\rightarrow 3(x-1)(x-1)$$

$$= \boxed{3(x-1)^2}$$

Objectives 1/31/18

- I can factor quadratic functions using GCF
- I can factor quadratic functions with $a = 1$, $a > 1$, and difference of squares

Turn in your homework on factoring!



Review of Factoring 1/31/18

Factoring Quadratic Expressions

$$ax^2+bx+c$$

To factor means to write an expression as the product of two or more expressions.

A quadratic expression is an algebraic expression in which the greatest exponent is 2.

Numeric

20

$= (4)(5)$

Algebraic

$x^2+9x+20$

$= (x+4)(x+5)$

Our goal when factoring is to similar to “undoing” the distributive property.

Factor x^2+bx+c (1-4)

To factor x^2+bx+c , you must find what two numbers multiply to c and add to b . If your two numbers are m and n , then $x^2 + bx + c = (x + m)(x + n)$.

1.

$$x^2 - 12x + 35$$

$$a = 1 \quad b = -12 \quad c = 35$$

$$(x - 7)(x - 5)$$

$$\begin{array}{r} 35 \\ -7 \quad -5 \\ -12 \end{array}$$

2.

$$x^2 + 8x + 15$$

$$a = 1 \quad b = 8 \quad c = 15$$

$$(x + 3)(x + 5)$$

$$\begin{array}{r} 15 \\ 3 \quad 5 \\ 8 \end{array}$$

3. $x^2 - 5x - 14$

$a=1 \quad b=-5 \quad c=-14$

$$(x+2)(x-7)$$

~~$$\begin{array}{cc} & -14 \\ 2 & -7 \\ & -5 \end{array}$$~~

4. $x^2 + 13x - 30$

$a=1 \quad b=13 \quad c=-30$

$$(x+15)(x-2)$$

~~$$\begin{array}{cc} & -30 \\ 15 & -2 \\ & 13 \end{array}$$~~

Factor $a^2 - b^2$ (5-9) Difference of Squares

To factor $a^2 - b^2$, a difference of squares, you just take the square roots of the terms.

These are the terms of each factor. One factor has +, and the other factor has -.

$$a^2 - b^2 = (a+b)(a-b)$$

$$5. x^2 - 9 = x^2 - 3^2$$

$$a = x$$

$$b = 3$$

$$(x+3)(x-3)$$

$$6. x^2 - 36 = x^2 - 6^2$$

$$(x+6)(x-6)$$

$$7. x^2 - 400$$

$$x^2 - 20^2$$

$$(x+20)(x-20)$$

$$4. \quad x^2 - 121 = x^2 - 11^2$$

$$= (x + 11)(x - 11)$$

$$5. \quad x^2 - 25$$

$$x^2 - 5^2$$

$$(x + 5)(x - 5)$$

HW Review

134

$$m^4 - 81$$

$$\sqrt{m^4} = m^2$$

$$\sqrt{81} = 9$$

$$(m^2 + 9)(m^2 - 9)$$

$$(m^2 + 9)(m + 3)(m - 3)$$

$$(13b) \quad 4b^2 - 400$$

$$\begin{array}{c} \downarrow \\ a = 2b \quad b = 20 \end{array}$$

$$(2b + 20)(2b - 20)$$

$$\underline{121}a^8 - 64b^4$$

$$a = 11a^{\textcircled{4}} \quad b = 8b^{\textcircled{2}}$$

$$\left((11a^4 + 8b^2) (11a^4 - 8b^2) \right)$$

Post-It**Check!!!**

Factor the following
difference of squares

$$4x^2 - 16$$

$$x^2 = x \cdot x$$

$$a^2 - b^2 = (a + b)(a - b)$$

$$\sqrt{4x^2} = 2x$$

$$\sqrt{16} = 4$$

$$(2x + 4)(2x - 4)$$

Post-It

Check!!!

Factor the following
difference of squares

$$9x^2 - 100$$

$$(3x + 10)(3x - 10)$$

$a > 1$ **Factoring Quadratics**

$$ac = -7$$

$$b = -6$$

$$14x^2 - 12x - 2 = 2(x-1)(7x+1)$$

$$2(7x^2 - 6x - 1)$$

1	-7	7x	-1
-7	-6	1	1
$7x^2$	$-7x$		
$1x$	-1		

How to Factor

- Check to see if you can factor out a GCF.
- Write the squared term in the top left box.
- Write the constant in the bottom right box.
- The missing diagonal sums to the middle term.
- The missing diagonal multiplies to the product of the other diagonal.
- Find the missing diagonal.
- Determine what was multiplied to form the four boxes.
- Rewrite with parentheses.

$$ac = -135$$

$$b = -6$$

$$9x^2 - 6x - 15 = (3x-5)(3x+3)$$

9	-135	-15	-6	$3x$	-5
		$9x^2$	$-15x$		
		$9x$	-15		

$$ac = -18$$

$$b = 3$$

$$2x^2 + 3x - 9 = (2x-3)(x+3)$$

6	-18	-3	3	$2x$	-3
		$2x^2$	$-3x$		
		$6x$	-9		

$$ac = 12$$

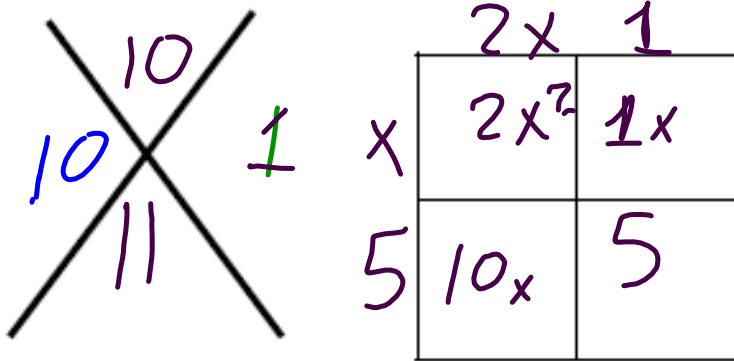
$$b = 8$$

$$3x^2 - 8x + 4 = (3x-2)(x-2)$$

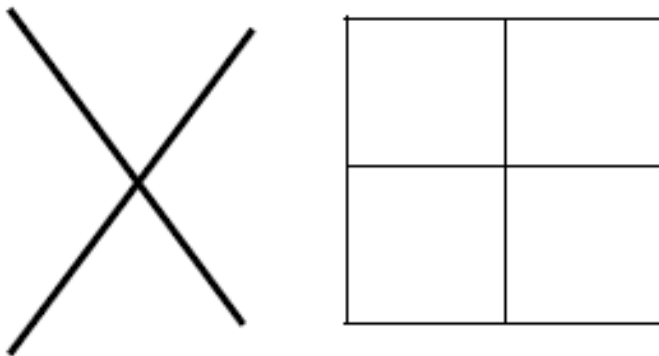
-6	-12	-2	-8	$3x$	-2
		$3x^2$	$-2x$		
		$-6x$	4		

$a=10$
 $b=11$

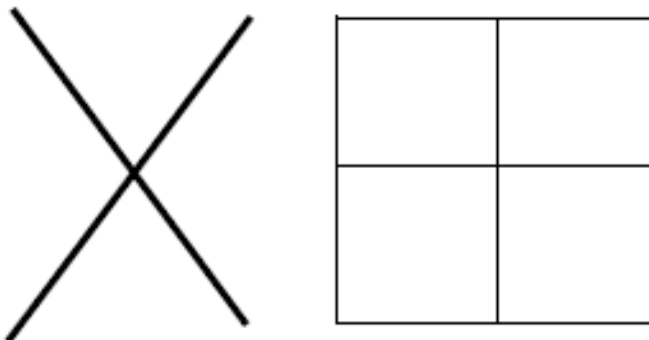
$$2x^2 + 11x + 5 = (2x + x)(1 + 5)$$



$$10x^2 + 80x + 70 = (\quad)(\quad)$$

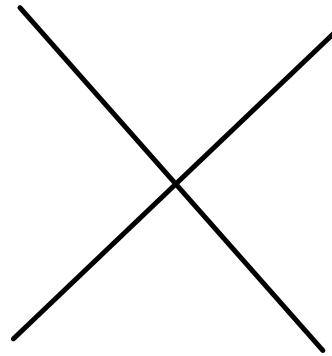


$$x^2 - 16 = (\quad)(\quad)$$

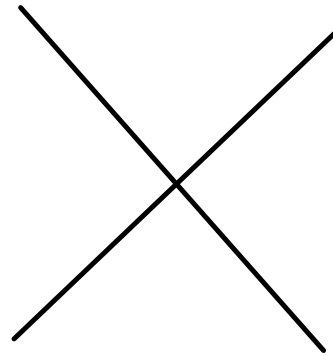


More Practice

1. $5x^2 - 45x + 40$



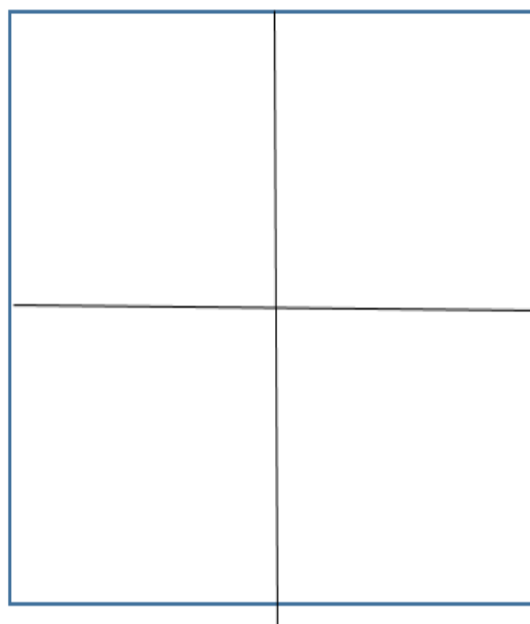
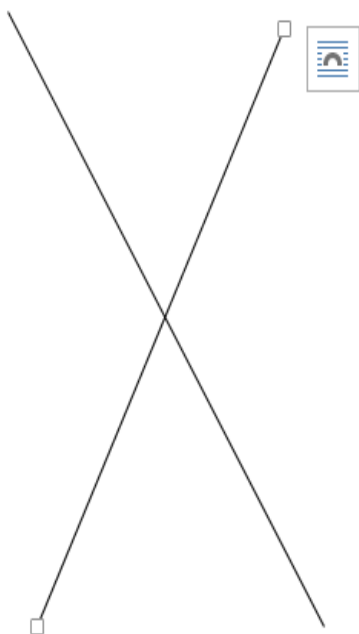
2. $3x^3 - 18x^2 - 24x$



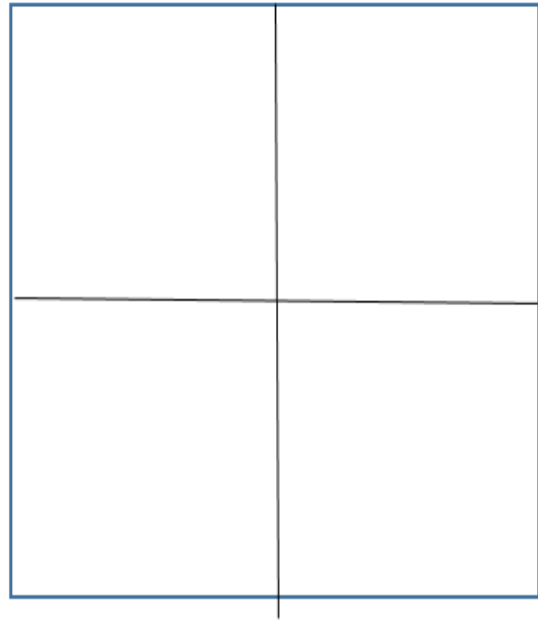
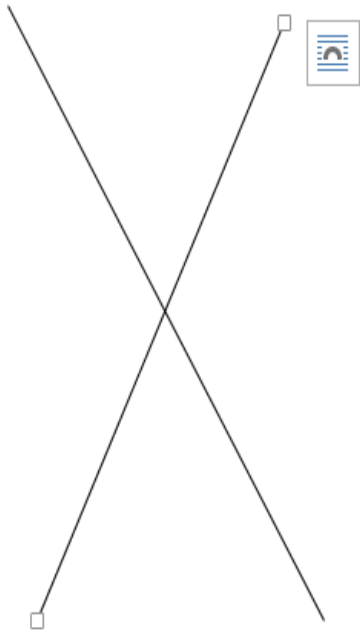
Factor ax^2+bx+c

To factor ax^2+bx+c , you must find what two numbers multiply to **ac** and add to **b**. Then draw the box and fill in with 1st and last term, then fill with **m** and **n**.

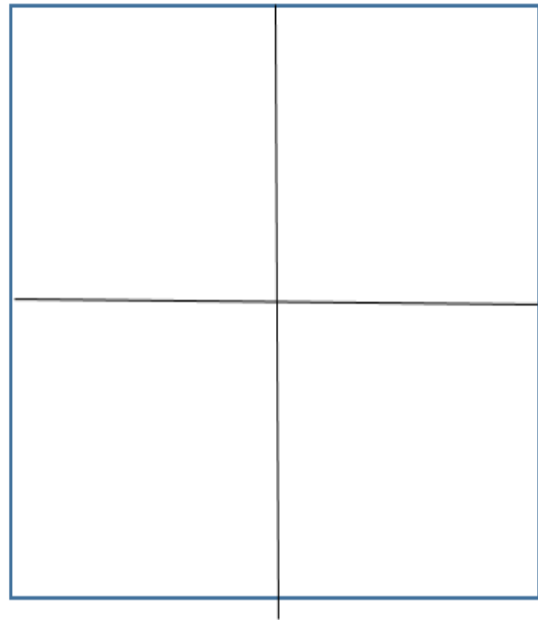
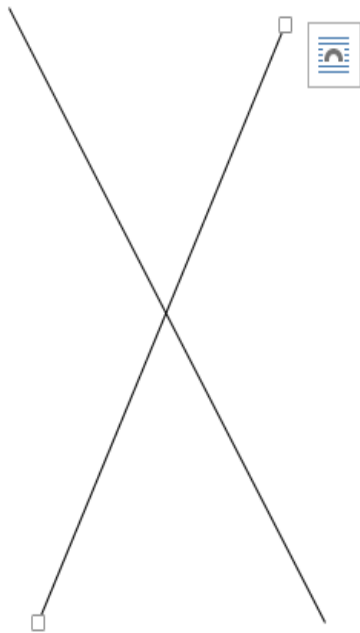
3. $11x^2 - 31x - 6$



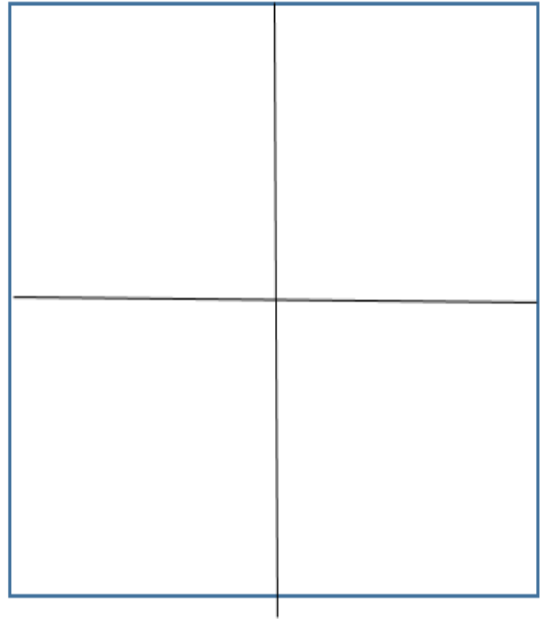
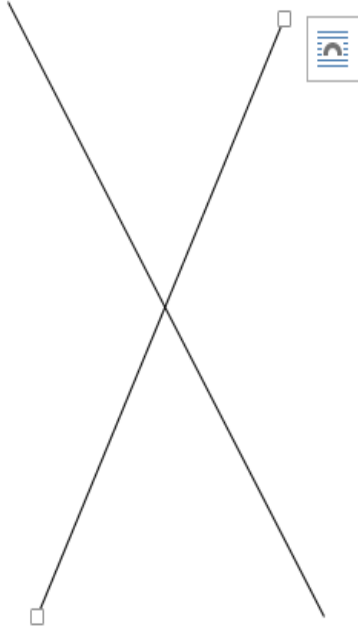
4. $7x^2 + 27x - 4$



5. $6x^2 + 7x - 5$



6. $2x^2 - 19x + 24$



Closing: Exit Ticket 1/31/18

Factor using GCF, Big X, and X-Box Methods.

1. $18x^2 - 6x$

2. $x^2 + 7x - 18$

3. $7x^2 - 13x - 2$
