

12/12/17

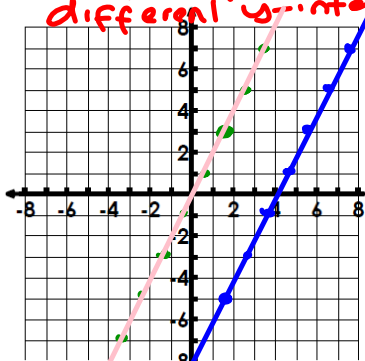
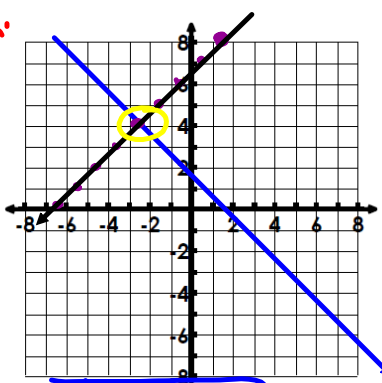
Good morning my dear students!

Bring out your Unit 2A Study Guide and let's continue from where we stopped.

You are taking the Unit 2A Test tomorrow!

Unit 2A Test Review 12/7/17

Systems of Equations and Inequalities Unit Review

What you need to know & be able to do	Things to remember	Examples	
1. Solve a system of linear equations by graphing.	Make sure each equation is solved for y. Graph both equations and find where they intersect.	1. Solve the system. $y = 2x + 3$ $y = 2x - 5$ <p style="color: red;">Same slope different y-intercept</p>  <p style="color: red;">No solution.</p>	2. Solve the system. $y = x + 8$ $m = \frac{1}{1} \quad b = 8$ $x = y - 8$ $y = -x$  <p style="color: blue; border: 1px solid blue; border-radius: 10px; padding: 5px;">(-4, 4)</p>

3. Solve the system of equations.

x	$y = x - 4$	$y = -x$
0	-4	0
1	-3	-1
2	-2	-2
3	-1	-3

 $(2, -2)$

4. Solve the system of equations.

x	$y = \frac{2}{5}x$	$y = -x - 7$
-10	-4	3
-5	-2	-2
0	0	-7
5	2	-12

 $(-5, -2)$

<p>2. Solve a system of linear equations using substitution.</p>	<p>Use only when one variable isolated</p> $10x - 7(-5x + 9) = -18$ $\underline{10x + 35x - 63 = -18}$ $45x - 63 = -18$ $\quad \quad \quad +63 \quad +63$ <hr/> $\underline{45x = 45}$ $\quad \quad \quad \underline{45} \quad \quad \quad \underline{45}$ $x = 1$	<p>5. Solve the system.</p> $y = -5x + 9$ $10x - 7y = -18$ $y = -5(1) + 9$ $y = 4$ $(1, 4)$
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6. Solve the system.

$$y = -8x - 16$$

$$y = 3x - 5$$

$$3x - 5 = -8x - 16$$

$$3x + 8x = -16 + 5$$

$$\frac{11x}{11} = \frac{-11}{11}$$

$x = -1$

$$y = 3(-1) - 5$$

$$y = -3 - 5$$

$$y = -8$$

$$(-1, -8)$$

3. Solve a system of linear equations using **elimination**.

$$\begin{aligned} 2(10) + y &= 19 \\ 20 + y &= 19 \\ y &= -1 \end{aligned}$$

$$(10, -1)$$

To eliminate a variable using addition or multiplication one coefficient must be positive and one must be negative.

7. Solve the system.

$$\begin{array}{r} x - y = 11 \\ + (2x + y = 19) \\ \hline 3x = 30 \\ \hline x = 10 \end{array}$$

$$\begin{array}{r} 10 - y = 11 \\ -10 \quad -10 \\ \hline -y = 1 \\ \hline y = -1 \end{array}$$

8. Solve the system.

$$4x = 20 - 8y$$

$$-4x + 2y = -30$$

$$\begin{array}{r} 4x + 8y = 20 \\ + (-4x + 2y = -30) \\ \hline \end{array}$$

$$\frac{10y}{10} = \frac{-10}{10}$$

$$y = -1$$

$$4x = 20 + 8$$

$$\frac{4x}{4} = \frac{28}{4}$$

$$x = 7$$

$$(7, -1)$$

9. Solve the system.

$$2x + 3y = 12$$

$$5x - y = 13 \quad | \cdot 3$$

$$\begin{array}{r} 15x - 3y = 39 \\ + (2x + 3y = 12) \\ \hline \end{array}$$

$$\frac{17x}{17} = \frac{51}{17}$$

$$x = 3$$

$$2(3) + 3y = 12$$

$$\begin{array}{r} 6 + 3y = 12 \\ -6 \quad -6 \\ \hline \end{array}$$

$$\frac{3y}{3} = \frac{6}{3}$$

$$y = 2$$

$$(3, 2)$$

10. Solve the system.

$$-3x - 8y = 0 \quad | \cdot 2$$

$$-2x - 10y = 14 \quad | \cdot -3$$

$$\begin{array}{r} -6x - 16y = 0 \\ + (6x + 30y = -42) \\ \hline \end{array}$$

$$\begin{array}{r} 14y = -42 \\ \hline 14 \quad 14 \end{array}$$

$$y = -3$$

$$-3x - 8(-3) = 0$$

$$-3x + 24 = 0$$

$$\begin{array}{r} -3x = -24 \\ \hline -3 \quad -3 \end{array}$$

$$x = 8$$

$$(8, -3)$$

4. Special Types of Systems	<p>No Solution:</p> <ul style="list-style-type: none">• False Equations• Slopes are the same• Y-intercepts are different• Parallel Lines <p>Infinite Solutions:</p> <ul style="list-style-type: none">• True Equations• Equations are the same• One Line	11. Solve the system: $y = 2x - 2$ $-2x + y = 1$ $y = 2x + 1$ $y = 2x - 2$ No solution
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12. Solve the system:

$$-9x - 3y = -18$$

$$3x + y = 6 \quad) \times 3$$

$$\begin{array}{r} 9x + 3y = 18 \\ + (-9x - 3y = -18) \\ \hline \end{array}$$

$$0 = 0$$

Infinitely many solutions.

<p>5. Systems with Real World Scenarios</p>	<p>Define your variables</p> <p>Determine if slope intercept or standard form is best</p> <p>Set up your equations and solve using elimination or substitution.</p> <p><u>Break Even Point:</u> where the cost equal the income</p>	<p>13. One high speed internet provider has a \$50 set up fee and costs \$30 per month. Another provider has no set up fee and costs \$40 per month. In how many months will both providers costs the same? What will that cost be?</p> <p>X: # of months. y: total cost of internet.</p> $y = 30x + 50$ $y = 40x$ $40x = 30x + 50$ $40x - 30x = 50$ $\frac{10x}{10} = \frac{50}{10}$ $X = 5$
	$y = 40(5)$ $y = 200$	
<p>In 5 months both providers will each cost \$200.</p>		

14. Sam spent \$24.75 to buy 12 flowers for his mother. Roses cost \$2.50 each and daisies costs \$1.75 each. How many of each flower type did he purchase?

X: Roses
y: daisies

$$\begin{aligned} X + y &= 12 \\ 2.50x + 1.75y &= 24.75 \end{aligned}$$

$$\begin{array}{r} -2.50x - 2.50y = -30 \\ + (2.50x + 1.75y = 24.75) \\ \hline -0.75y = -5.25 \\ \hline -0.75 \quad -0.75 \\ \hline \end{array}$$

$$y = 7$$

$$\begin{array}{r} X + y = 12 \\ -7 \quad -7 \\ \hline X = 5 \end{array}$$

5 roses
7 daisies

15. Explain what a break-even point is.

$$\text{Cost} = \text{Income}$$

What will the income and cost always be at the break-even point?

Same Amount.

What is the profit at the break-even point?

$$y = 12(60)$$

$$y = 720 \quad \$720$$

16. As a fundraiser for a band trip, AHS plans to sell hats with the school logo. The company producing the hats charges \$240 for the design and set up plus \$8 per hat. The band members will sell the hats for \$12 each. What is the break-even point? What will the cost and income be?

$$\text{Cost: } y = 8x + 240$$

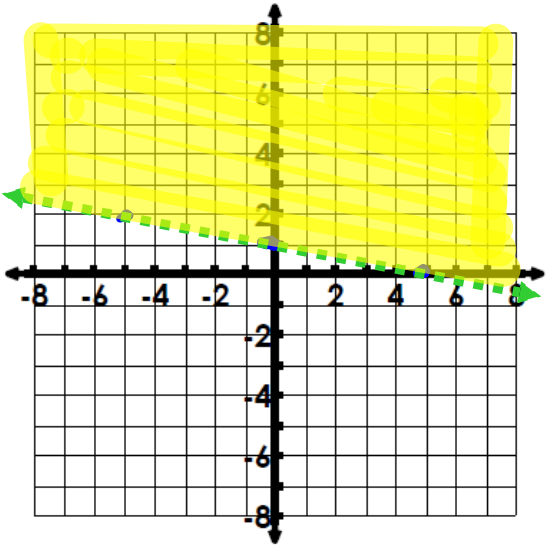
$$\text{Income: } y = 12x$$

$$12x = 8x + 240$$

$$12x - 8x = 240$$

$$\frac{4x}{4} = \frac{240}{4}$$

$$x = 60 \text{ hats}$$

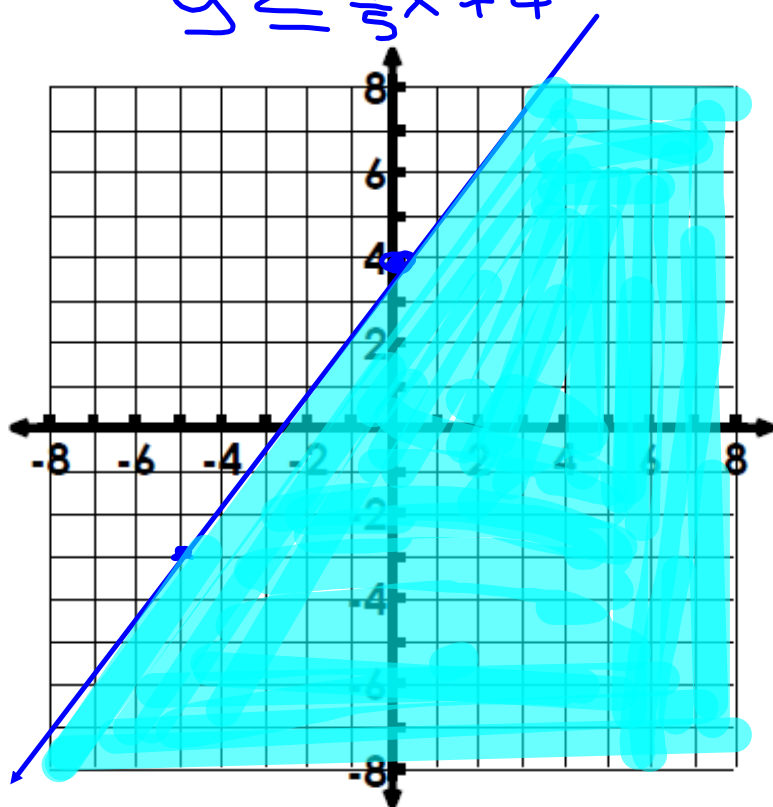
<p>6. Graph a linear inequality</p> <p>$m = -\frac{1}{5}$</p> <p>$b = 1$</p>	<p>Make sure equation is solved for y</p> <p>Graph the line</p> <p>Determine if dashed or solid</p> <p>Determine whether to shade below or above the line</p> <p>*Golden Rule of Inequalities can apply here.</p>	<p>17. Graph $y > -\frac{1}{5}x + 1$</p> 
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18. $7x - 5y \geq -20$

$$\begin{array}{r} -7x \quad -7x \\ \hline -5y \geq -7x - 20 \\ \hline y \leq \frac{7}{5}x + 4 \end{array}$$

$$m = \frac{7}{5}$$

$$b = 4$$



7. Solve a system of linear inequalities by **graphing**.

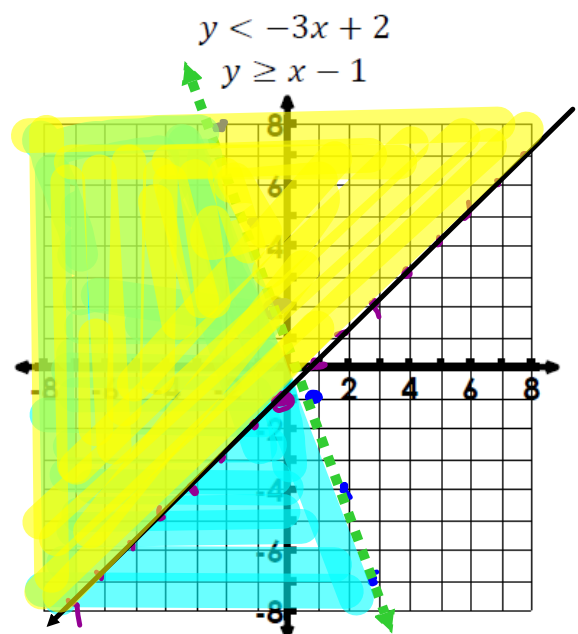
Determine if you have a solid or dashed line

Then determine whether to shade above or below.

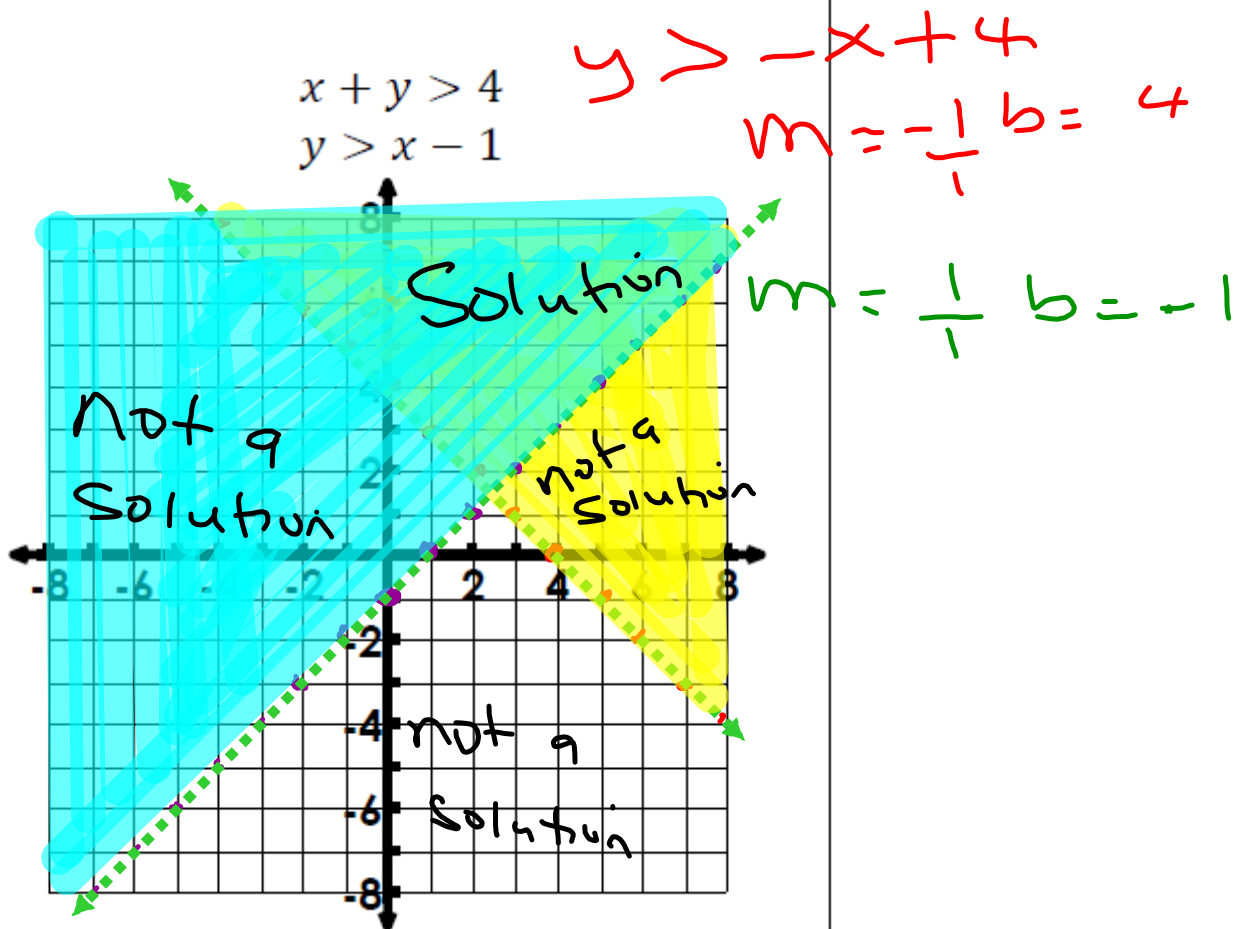
Find the region where the shading overlapped.

$$m = -\frac{3}{1} \quad b = 2$$
$$m = \frac{1}{1} \quad b = -1$$

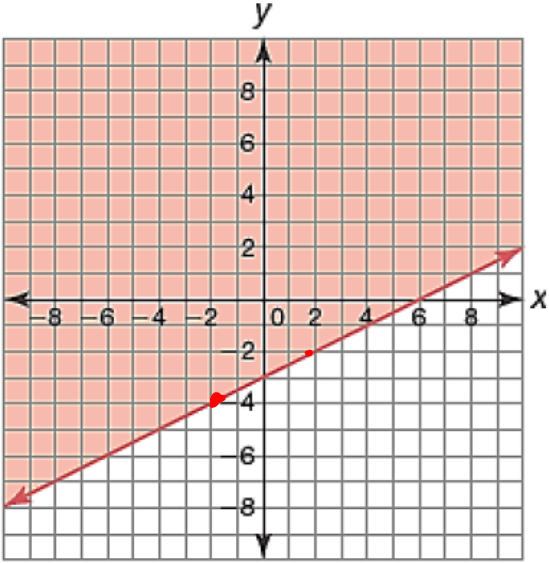
19. Solve the system. Label the different regions as solution or not a solution.



20. Solve the system. Label the different regions as solution or not a solution.



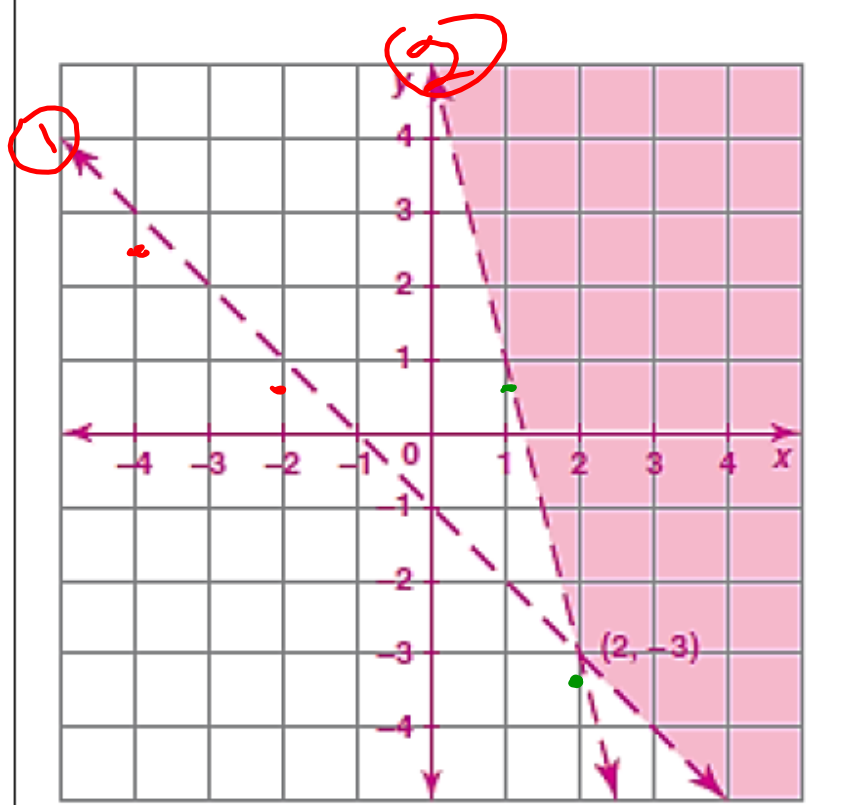
8. Real World with Systems of Inequalities		<p>21. Write a system to describe: The maximum capacity for an elevator is <u>15</u> people and <u>3000</u> pounds. It is estimated that adults weight <u>200</u> pounds and children under 16 weight <u>100</u> pounds.</p> <p>x: adults y: children</p> $x + y \leq 15$ $200x + 100y \leq 3000$	<p>22. Write a system to describe: Jada is selling tickets to SouthCobb's production of Footloose. SouthCobb's theater holds at most <u>700</u> people. Children's tickets are <u>\$6.00</u> and adult tickets are <u>\$10.00</u>. She hopes to sell at least \$500 worth of tickets.</p> <p>x: children y: adult</p> $x + y \geq 700$ $6x + 10y \geq 500$
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<p>9. Naming Linear Inequalities and Systems</p>	<p>Identify:</p> <ul style="list-style-type: none">*Slope*Y-intercept*Type of Line*Shading <p>$m: \frac{2}{4} = \frac{1}{2}$</p> <p>$b: -3$</p> <p><u>W</u></p>	<p>23. Name the inequality.</p> 
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24. Name the system of inequalities.

① $m = -\frac{1}{1}$ $b = -1$ ✓

② $m = -\frac{4}{1}$ $b = 5$ ✓



$$y = .50x + 4$$

Multiple Choice Practice

$$y = .25x + 5$$

25. Taxi Company A charges \$4 plus \$0.50 per mile. Taxi Company B charges \$5 plus \$0.25 per mile. Which system best represents this problem?

(a) $Y = 4x + 0.5$

(b) $Y = 4x + 0.25$

$Y = 5x + 0.25$

$Y = 5x + 0.5$

(c) $Y = 0.5x + 4$

(d) $Y = 0.5x + 5$

$Y = 0.25x + 5$

$Y = 0.25 + 4$

26. The Fun Guys game rental store charges an annual fee of \$5 plus \$5.50 per game rented. The Game Bank charges an annual fee of \$17 plus \$2.50 per game. For how many game rentals will the cost be the same at both stores? What is the cost?

(a) ~~Month 10; 550~~

(b) ~~Month 8; 580~~

(c) ~~Month 9; 580~~

(d) ~~Month 11; 550~~

$$2.50(4) + 17$$

$$10 + 17$$

$$y = 27$$

$$y = 5.50x + 5$$
$$y = 2.50x + 17$$

$$\begin{array}{r} 5.50x + 5 = 2.50x + 17 \\ -2.50x \qquad \qquad -2.50x \\ \hline 3.00x + 5 = 17 \\ \quad \quad \quad -5 \quad - \\ \hline 3.00x \qquad \qquad 12 \\ \underline{3.00} \qquad \quad \underline{3.00} \quad x=4 \end{array}$$

27. Solve the system of equations:
- $$4x - 4y = -16$$
- $$x - 2y = -12$$

(a) (8, -4)
(c) (4, 8)

(b) (-2, 4)
(d) (4, -8)

28. Which point is a solution of the system:
- $$2x + y \geq 3$$
- $$y \geq -2x + 1$$

(a) (0, 0) X
(c) (0, 1) X

$2 + 0 \geq 3$ X (b) (1, 0)
(d) (1, 1)

$$1 \geq -2 + 1$$

$$1 \geq -1 \checkmark$$

$$4x - 4y = -16$$

$$(x - 2y = -12) \cdot 4$$

~~$$4x - 4y = -16$$~~

~~$$4x + 8y = 48$$~~

$$\frac{4y}{4} = \frac{32}{4}$$

$$\boxed{y = 8}$$

$$4x - 4(\widehat{8}) = -16$$

$$4x - 32y = -16$$

$$\begin{array}{r} +32 \\ +32 \end{array}$$

$$\frac{4x}{4} = \frac{16}{4}$$

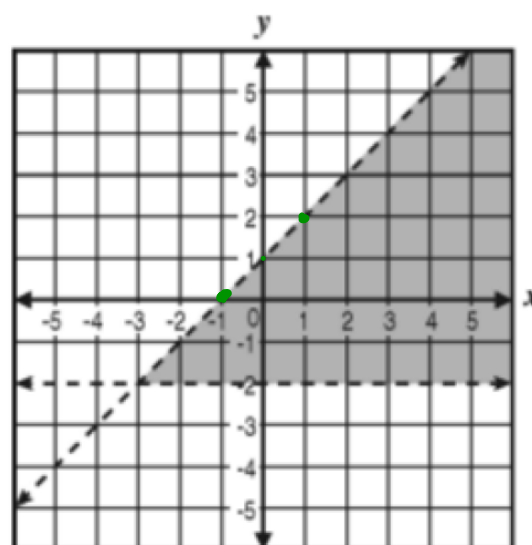
$$\boxed{x = 4}$$

$$(4, 8)$$

29. Which system of inequalities best describes the graph?

- (a) $y > -2$
 $y > x + 1$
- (b) $y < -2$
 $y > x + 1$
- (c) $y > -2$
 $y < x + 1$
- (d) $y < -2$
 $y < x + 1$

$$y < x + 1$$
$$y > -2$$



30. The graph to the right shows the cost of two phone plans. How many minutes does a person need to call each month so that Plan B is the less expensive plan to use?
- (a) Less than 10 minutes
 - (b) Less than 40 minutes
 - (c) More than 40 minutes
 - (d) More than 30 minutes but less than 40 minutes

Use the graph below to answer the question.



31. A student store sold a total of 55 shirts for \$620. The shirts sold were either red or white. If the red shirts sold for \$12 each and the white sold for \$10 each, how many of each color shirt were sold?

- (a) 20 red, 35 white (b) 27 red, 28 white
 (c) 28 red, 27 white (d) 35 red, 20 white


$x \quad y$

$$x + y = 55$$

$$12x + 10y = 620$$

32. Consider each system of equations below. Just by looking at the equations, tell how many solutions the system will have and explain why.


a. $\begin{cases} y = 4x - 3 \\ y = 4x + 2 \end{cases}$

No solution
parallel lines


b. $\begin{cases} y = \frac{1}{3}x + 5 \\ y = \frac{1}{3}x + 5 \end{cases}$

Same slope
Same y-int.
Infinitely many
Solutions
One line.

c. $\begin{cases} y = -x + 2 \\ y = \frac{1}{3}x + 6 \end{cases}$

Different slopes
different y-int
One solution


d. $\begin{cases} y = -\frac{3}{4}x + 5 \\ y = -\frac{3}{4}x - 4 \end{cases}$

Same slope
diff. y-int
No solution
parallel lines.